



Model Answer: Winter - 2019

Subject: Applied Mechanics

Sub. Code: 22203

Important Instructions to examiners:

- 1) The answers should be examined by key words and not as word-to-word as given in the model answer scheme.
- 2) The model answer and the answer written by candidate may vary but the examiner may try to assess the understanding level of the candidate.
- 3) The language errors such as grammatical, spelling errors should not be given more importance. (Not applicable for subject English and Communication Skills.)
- 4) While assessing figures, examiner may give credit for principal components indicated in the figure. The figures drawn by the candidate and those in the model answer may vary. The examiner may give credit for any equivalent figure drawn.
- 5) Credits may be given step wise for numerical problems. In some cases, the assumed constant values may vary and there may be some difference in the candidate's answers and the model answer.
- 6) In case of some questions credit may be given by judgment on part of examiner of relevant answer based on candidate's understanding.
- 7) For programming language papers, credit may be given to any other program based on equivalent concept.

Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
Q. 1		Attempt any <u>FIVE</u> of the following:		10
	a) Ans.	Define Scalar and Vector quantity. Scalar Quantity: A physical quantity having only magnitude but no direction is called as scalar quantity.	1	
		Vector Quantity: A physical quantity having both magnitude as well as direction is called as vector quantity.	1	2
	b) Ans.	State VR of geared pulley block. $V.R. = \frac{N_1}{N_2} \times \frac{N_3}{N_4}$ Where, N ₁ = Number of cogs on effort wheel. N ₂ = Number of teeth on pinion wheel. N ₃ = Number of teeth on spur wheel. N ₄ = Number of cogs on load wheel.	1	2
		OR		
		$V.R. = \frac{D}{d} \times \frac{N_3}{N_2}$ Where, D = Diameter of effort wheel. D = Diameter of load wheel. N ₂ = Number of teeth on pinion wheel. N ₃ = Number of teeth on spur wheel.	1	2

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Q. 1	c)	State Law of polygon of forces.	1		
	Ans.	This law states that, "If number of coplanar concurrent forces acting simultaneously on a body, be represented in magnitude and direction by the sides of polygon taken in same order, then their resultant may be represented in magnitude and direction by the closing side of the polygon, taken in opposite order."			
		<p>(a) Space diagram</p> <p>(b) Vector diagram</p>	1	2	
	d)	Define free body diagram.	2	2	
	Ans.	When all active and reactive forces acting on the free body are shown and thus the diagram obtained is called as 'free body diagram'.			
	e)	State four laws of static friction.	<ol style="list-style-type: none"> The frictional force is always acts tangential to the plane of contact and in the opposite direction of motion. When the body is in limiting equilibrium, the ratio of limiting friction to normal reaction is constant. This ratio is called as 'coefficient of friction'. The coefficient of friction depends upon the nature of surfaces in contact and is not dependent on surface areas in contact. The static friction is more than dynamic friction. Force of friction is a self-adjusting force and it increases as the applied force increases up to limiting friction. 	1/2 each (any four)	2
f)	State the centroid of semi-circle and show it on the sketch.	$\bar{X} = R$ $\bar{Y} = \frac{4R}{3\pi} \text{ (from base AB)}$		1/2	2
Ans.	Centroid of semi-circle :			1/2	
				1	

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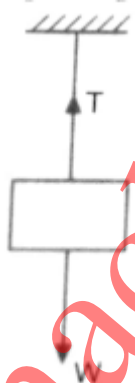
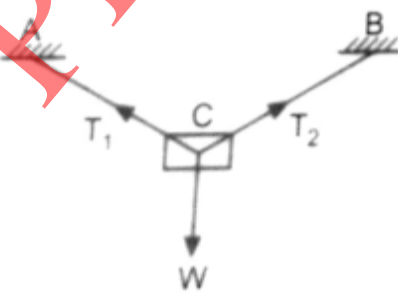
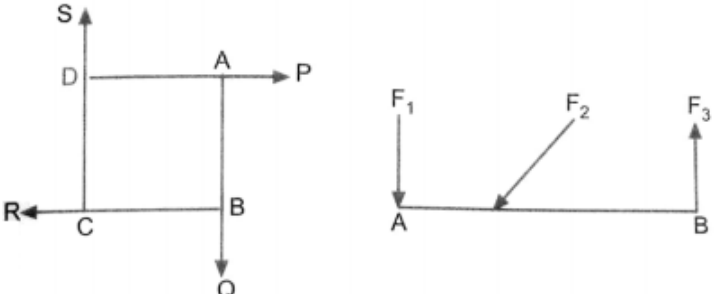
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Q. 1	g) Ans.	State two limitations of Lami's theorem. 1. The theorem is applicable only if the body is in equilibrium. 2. The theorem is not applicable for parallel or non-concurrent force system. 3. The theorem is not applicable for more or less than three concurrent forces. 4. The theorem is not applicable for non-coplanar forces.	1 each (any two)	2

Pinnacle

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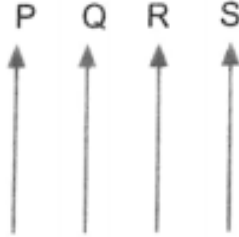

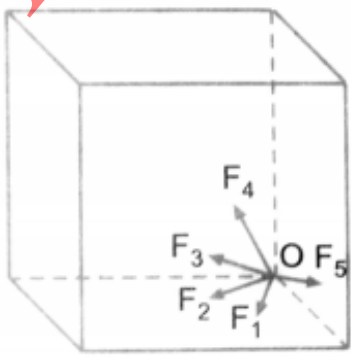
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Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
Q. 2	a)	<p>Attempt any <u>THREE</u> of the following:</p> <p>Define force system. Explain three force systems with sketches.</p> <p>When two or more forces acting on a body, they are said to form a system of forces or force system.</p> <p>Force systems with sketches:</p> <p>1. Coplanar Collinear force system: The force system in which forces lies on the same plane and act along the same line of action are known as Coplanar Collinear force system.</p>  <p>2. Coplanar Concurrent force system: The force system in which forces lies on the same plane and meet at a point are known as Coplanar Concurrent force system.</p>  <p>3. Coplanar Non-concurrent force system: The force system in which forces lies on the same plane but meet at different points are known as Coplanar Concurrent force system.</p> 	1	12

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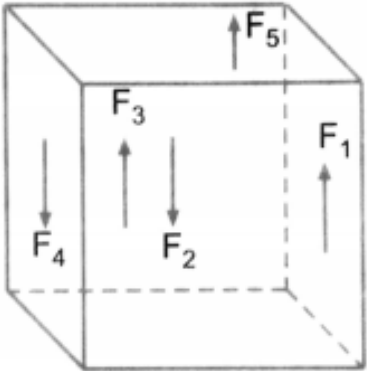
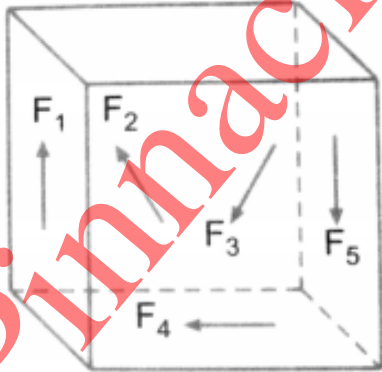
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Q. 2	a) Ans.	<p>4. Coplanar parallel force system:</p> <p>(i) Like parallel force system: The force system in which forces lies on the same plane and are parallel to each other acting in same direction are known as Coplanar Like parallel force system.</p>  <p>(ii) Unlike parallel force system: The force system in which forces lies on the same plane and are parallel to each other but acting in opposite direction are known as Coplanar Unlike parallel force system.</p>  <p>5. Non-coplanar concurrent force system: The force system in which forces lies in different planes but meet at a point are known as Non-coplanar Concurrent force system.</p> 		

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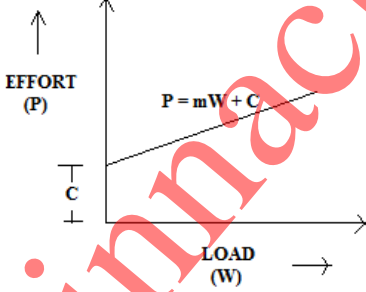
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Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
Q. 2	a) Ans.	<p>6. Non-coplanar parallel force system: The force system in which forces lies in different planes but are parallel to each other are known as Non-coplanar parallel force system.</p>  <p>7. General force system: The force system in which forces act in different planes and they do not possess one single point of concurrency are known as General force system.</p>  <p>(Note: Definition 1 mark and any Three force system 1mark each).</p>	1 each (any three)	4
	b) Ans.	<p>For a certain machine, VR is 125. To lift a load of 11.90 kN, an effort of 190 N is required. Calculate the effort required to lift a load of 72 kN and identify the type of machine.</p> $MA = \frac{W}{P} = \frac{11.90 \times 10^3}{190} = 62.63$ $\eta = \frac{MA}{VR} \times 100 = \frac{62.63}{125} \times 100 = 50.10\%$ <p>Since η of machine is $> 50\%$, the machine is reversible.</p> <p>Effort required to lift a load of 72 kN</p> $\eta = \frac{MA}{VR} \times 100 = \frac{W/P}{VR} \times 100$	1 1 1	

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Q. 2	b)	$50.10 = \frac{72 \times 10^3}{125} \frac{1}{P} \times 100$ $P = 1149.70 \text{ N}$	1	4
	c)	<p>State law of machine and explain its significance.</p>		
	Ans.	<p>Law of machine: The relation between the load lifted (W) and the effort applied (P) is known as the law of machine. This relationship, when plotted on a graph results in a straight line as shown below. The equation of this straight line is,</p> $P = (mW + C) \text{ N}$  <p>Where, m = Slope of line = constant c = Intercept on y axis = effort required to start the machine.</p>	1	
		<p>Significance of law of machine: With the help of law of machine one can find effort required to lift any given load and vice versa.</p>	1	4
	d)	<p>State four laws of static friction.</p>		
	Ans.	<ol style="list-style-type: none"> The frictional force is always acts tangential to the plane of contact and in the opposite direction of motion. When the body is in limiting equilibrium, the ratio of limiting friction to normal reaction is constant. This ratio is called as 'coefficient of friction'. The coefficient of friction depends upon the nature of surfaces in contact and is not dependent on surface areas in contact. The static friction is more than dynamic friction. Force of friction is a self-adjusting force and it increases as the applied force increases up to limiting friction. 	1 each (any four)	4

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Q. 3	a)	<p>Attempt any THREE of the following:</p> <p>Calculate the magnitude and direction of resultant for the concurrent force system as shown in figure No. 1. Show it on the sketch. Use analytical method only.</p> <p style="text-align: center;">Fig. No. 1</p>		12
	Ans.	<p>1) Resolving all forces</p> $\Sigma F_x = +(10\cos 30^\circ) - (25\cos 50^\circ) - (15\cos 40^\circ) + 5$ $= -13.90 \text{ kN.}$ $\Sigma F_y = -(10\sin 30^\circ) - (25\sin 50^\circ) + (15\sin 40^\circ)$ $= -14.51 \text{ kN.}$ <p>2) Magnitude of Resultant</p> $R = \sqrt{(\Sigma F_x)^2 + (\Sigma F_y)^2} = \sqrt{(-13.90)^2 + (-14.51)^2}$ $R = 20.09 \text{ kN.}$ <p>3) Direction of Resultant</p> $\theta = \tan^{-1} \left \frac{\Sigma F_y}{\Sigma F_x} \right = \tan^{-1} \left \frac{14.51}{13.90} \right $ $\theta = 46.23^\circ$ <p>4) Position of Resultant</p> <p>Since ΣF_x is -ve and ΣF_y is -ve, Resultant lies in Third quadrant.</p>	1 1 1	4

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Q. 3	b)	<p>State law of polygon of forces and explain it with sketch.</p> <p>This law states that, "If number of coplanar concurrent forces acting simultaneously on a body, be represented in magnitude and direction by the sides of polygon taken in same order, then their resultant may be represented in magnitude and direction by the closing side of the polygon, taken in opposite order."</p> <p>(a) Space diagram (b) Vector diagram</p> <p>Consider four forces $F_1 = AB$, $F_2 = BC$, $F_3 = CD$, and $F_4 = DE$ acting at a point 'O' as shown in space diagram. Label all the forces by Bow's notation.</p> <p>Considering suitable scale for vector diagram and find vector length for different forces.</p> <p>Draw vector $ab \parallel AB$, $bc \parallel BC$, $cd \parallel CD$, and $de \parallel DE$ as shown in the vector diagram to represent the forces F_1, F_2, F_3, and F_4 respectively. $abcde$ is an open polygon. Join the first point 'a' and last point 'e'. The closing side 'ae' of the polygon represents the resultant of all the forces in magnitude and direction. In space diagram, through 'O' draw line parallel to 'ae' to locate the position of the resultant. Measure angle 'θ', which gives the direction of resultant with the horizontal.</p>	1 1	
	c)	<p>In a worm and worm wheel, the number of teeth on the worm wheel is 120. The diameter of effort wheel is 100mm and that of loading drum is 150mm. This worm and worm wheel lifts a load of 2.5 kN by applying 100 N effort. Calculate efficiency and effort lost in friction.</p>	2	4
	Ans.	<p>Number of teeth on worm wheel (T) = 120.</p> <p>Radius of effort wheel (R) = $\frac{D}{2} = \frac{100}{2} = 50$ mm</p> <p>Radius of load drum (r) = $\frac{d}{2} = \frac{150}{2} = 75$ mm</p> <p>1) Efficiency of worm and worm wheel</p>		



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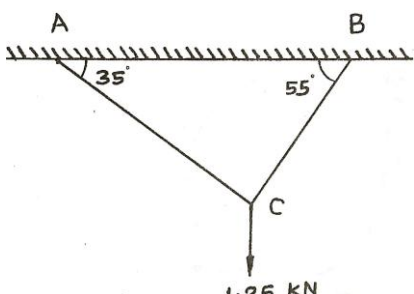
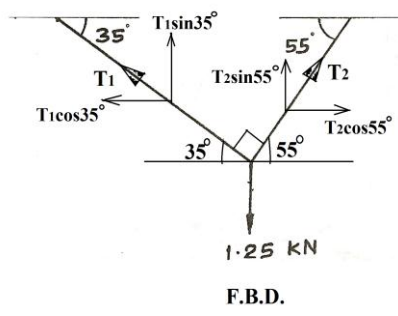
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Q. 3	c)	<p>Mechanical Advantage (MA) = $\frac{W}{P} = \frac{2.5 \times 10^3}{100} = 25$</p> <p>Velocity Ratio (VR) = $\frac{RT}{r} = \frac{50 \times 120}{75} = 80$</p> <p>$\eta = \frac{MA}{VR} \times 100 = \frac{25}{80} \times 100 = 31.25\%$</p> <p>2) Effort lost in friction</p> <p>$P_f = P - P_i$</p> <p>$= P - \frac{W}{VR} = 100 - \frac{2.5 \times 10^3}{80}$</p> <p>$P_f = 68.75 \text{ N}$</p>	1 1 1 1	4
	d)	<p>A machine lifts a load of 19kN and 29kN by efforts of 700N and 900N respectively. Calculate the law of machine and efficiency of a load of 50kN if VR is 50.</p> <p>Ans.</p> <p>1) Law of machine</p> <p>Law of machine is</p> <p>$P = mW + C$</p> <p>$700 = m(19000) + C \dots\dots\dots(i)$</p> <p>$900 = m(29000) + C \dots\dots\dots(ii)$</p> <p>Subtracting equation (1) from (2)</p> <p>$m = 0.02$</p> <p>Putting value of m in equation (1),</p> <p>$700 = (0.02 \times 19000) + C$</p> <p>$C = 320 \text{ N}$</p> <p>Hence, law of machine is, $P = (0.02)W + 320 \text{ N}$</p> <p>2) Efficiency at load of 50kN</p> <p>$P = 0.02 \times 50000 + 320$</p> <p>$= 1320 \text{ N}$</p> <p>$\eta = \frac{MA}{VR} \times 100 = \frac{W/P}{VR} \times 100$</p> <p>$= \frac{50000/1320}{50} \times 100$</p> <p>$= 75.76\%$</p>	1/2 1/2 1 1	4

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Q. 4	b)	  <p>Fig. No. 2</p> <p>F.B.D.</p> <p>Using the conditions of equilibrium for concurrent force system and resolving all forces:</p> $\Sigma F_x = 0$ $T_2 \cos 55^\circ - T_1 \cos 35^\circ = 0$ $0.57 T_2 - 0.82 T_1 = 0 \dots\dots\dots (i)$ $\Sigma F_y = 0$ $T_2 \sin 55^\circ + T_1 \sin 35^\circ - 1.25 = 0$ $0.82 T_2 + 0.57 T_1 - 1.25 = 0 \dots\dots\dots (ii)$ <p>Solving equation (i) and (ii) simultaneously</p> $T_1 = 0.717 \text{ kN}$ $T_2 = 1.024 \text{ kN}$	1	
			1	
			1	
			1	4

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	c)	<p>A beam is loaded as shown in figure No. 3. Calculate its support reactions using graphical method only.</p> <p>Fig. No. 3</p> <p>FOR SPACE DIAGRAM Scale: 1cm = 1m</p> <p>SPACE DIAGRAM</p> <p>FUNICULAR POLYGON</p> <p>FOR VECTOR/POLAR DIA. Scale: 1cm = 200N.</p> <p>VECTOR/POLAR DIAGRAM</p> <p> $R_A = 1(p_s) \times \text{scale}$ $= 2.075 \times 200$ $R_A = 415 \text{ N}$ </p> <p> $R_B = 1(rs) \times \text{scale}$ $= 2.425 \times 200$ $R_B = 485 \text{ N}$ </p> <p>(Note: Answer may vary by $\pm 2 \text{ N}$)</p>	1 1 1	4
	d)	<p>A body weighing 250N is resting on a rough horizontal plane and is just moved by a horizontal force of 100 N. Calculate coefficient of friction. Also calculate magnitude and direction of the resultant reaction.</p> <p>Ans. For limiting equilibrium</p> <p>$\Sigma F_x = 0$</p> <p>$100 - F = 0$</p>		

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Q. 4	e)	<p>Applying Lami's theorem at 'O'</p> $\frac{R_A}{\sin 10^\circ} = \frac{R_B}{\sin 90^\circ} = \frac{750}{\sin 100^\circ}$ $R_A = \sin 10^\circ \times \frac{750}{\sin 100^\circ} = 132.25 \text{ kN}$ $R_B = \sin 90^\circ \times \frac{750}{\sin 100^\circ} = 761.57 \text{ kN}$ <p style="text-align: center;">OR</p> <p style="text-align: center;">Fig. No. 4</p> <p style="text-align: center;">F.B.D.</p> <p>Using the conditions of equilibrium for concurrent force system and resolving all forces –</p> $\Sigma F_x = 0$ $R_A - R_B \cos 80^\circ = 0$ $R_A - 0.174 R_B = 0 \dots\dots\dots (i)$ $\Sigma F_y = 0$ $R_B \sin 80^\circ - 750 = 0$ $R_B = 761.57 \text{ kN}$ <p>Put this value in equation no.(i)</p> $R_A - 0.174 \times 761.57 = 0$ $R_A = 132.51 \text{ kN}$	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p>	<p>4</p>

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Q. 5	c)	<p>Resolution of Forces</p> $\Sigma F_x = - (100\cos 35^\circ) + 500 = + 418.08 \text{ N}$ $\Sigma F_y = + (100\sin 35^\circ) + 500 - 300 = + 257.36 \text{ N}$ <p>Magnitude of resultant</p> $R = \sqrt{(\Sigma F_x)^2 + (\Sigma F_y)^2} = \sqrt{(418.08)^2 + (257.36)^2}$ <p>R = 490.94 N.</p> <p>Direction of Resultant</p> $\theta = \tan^{-1} \left \frac{\Sigma F_y}{\Sigma F_x} \right = \tan^{-1} \left \frac{257.36}{418.08} \right $ <p>$\theta = 31.62^\circ$ with the positive X-axis in First quadrant.</p> <p>Position of Resultant (from A)</p> <p>According to the Varignon's theorem</p> $\Sigma MFA = MRA$ <p>Let resultant lies at 'x' perpendicular distance from point 'A'</p> $+(300 \times 5) - (500 \times 2.5) = R \times x$ $250 = 490.94 \times x$ $x = 0.51 \text{ m}$ <p>As the value of ΣMFA is +ve, therefore resultant should produce 'clockwise moment' about 'A' point at a perpendicular distance of $x = 0.51 \text{ m}$ as shown in figure below.</p>	1 1 1 1 1	6

Que. No.	Sub. Que.	Model Answers	Marks	Total Marks
Q. 6	c)	<p>Locate the center of gravity for the solid as shown in Figure No. 9.</p> <p>Fig. No. 9</p>	1	
	Ans.	<p>Let, Fig. 1 = Cylinder and Fig. 2 = Sphere.</p> <p>1) Volume calculations</p> <p>$V_1 = \text{Volume of Cylinder}$ $= \pi R^2 h = \pi (150)^2 \times 400$ $= 28.274 \times 10^6 \text{ mm}^3$</p> <p>$V_2 = \text{Volume of Sphere}$ $= \frac{4}{3} \pi R^3 = \frac{4}{3} \pi (100)^3 = 4.188 \times 10^6 \text{ mm}^3$</p> <p>$V = V_1 + V_2 = 28.274 \times 10^6 + 4.188 \times 10^6 = 32.462 \times 10^6 \text{ mm}^3$</p> <p>2) \bar{X} calculation</p> <p>As the given composite solid is symmetric about Y-Y axis, CG lies on the axis of symmetry.</p> <p>$\bar{X} = \frac{D}{2} = \frac{300}{2} = 150 \text{ mm}$</p> <p>(3) \bar{Y} calculation</p> <p>$y_1 = \frac{h}{2} = \frac{400}{2} = 200 \text{ mm}$</p> <p>$y_2 = 400 + \text{radius of sphere} = 400 + 100 = 500 \text{ mm}$</p> <p>$\bar{Y} = \frac{V_1 y_1 + V_2 y_2}{V} = \frac{(28.274 \times 10^6 \times 200) + (4.188 \times 10^6 \times 500)}{32.462 \times 10^6}$</p> <p>$\bar{Y} = 238.703 \text{ mm}$</p>	1 1 1 1	6